

# Status of the Super B Project and Beam Polarization Issues

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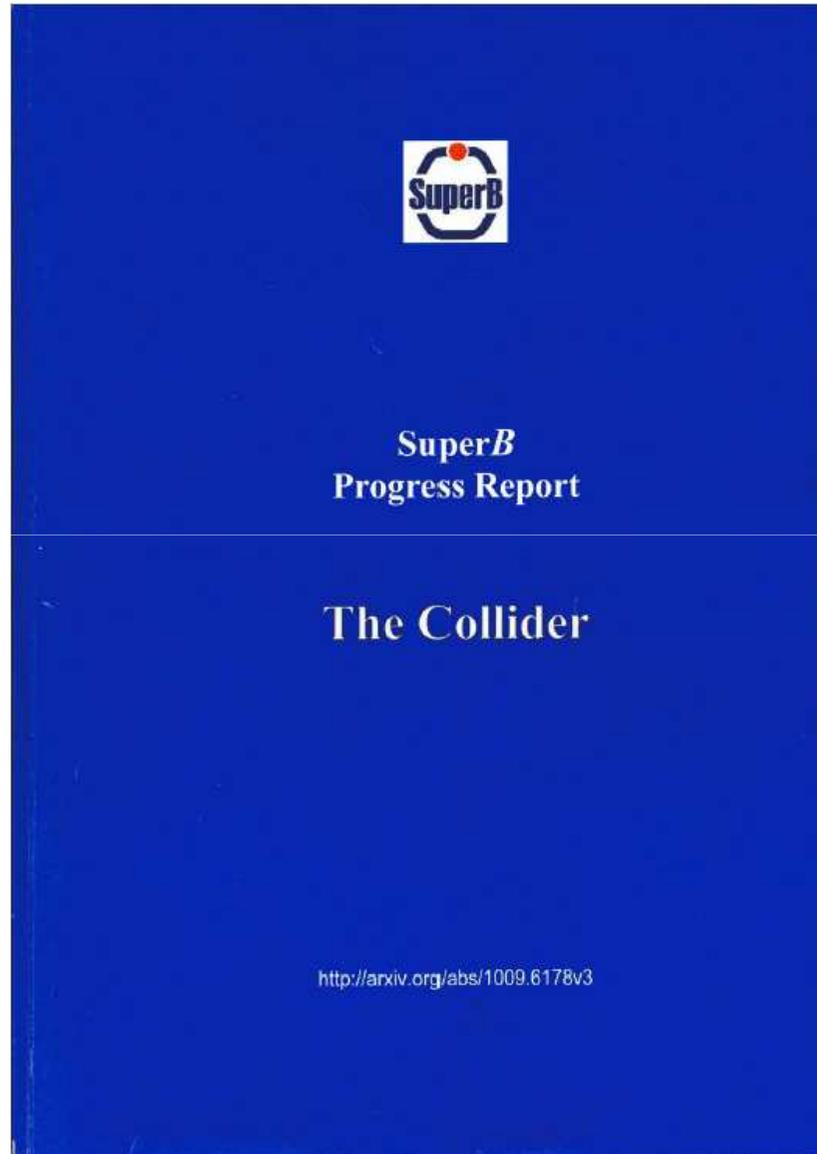
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# Present status – Blue Book



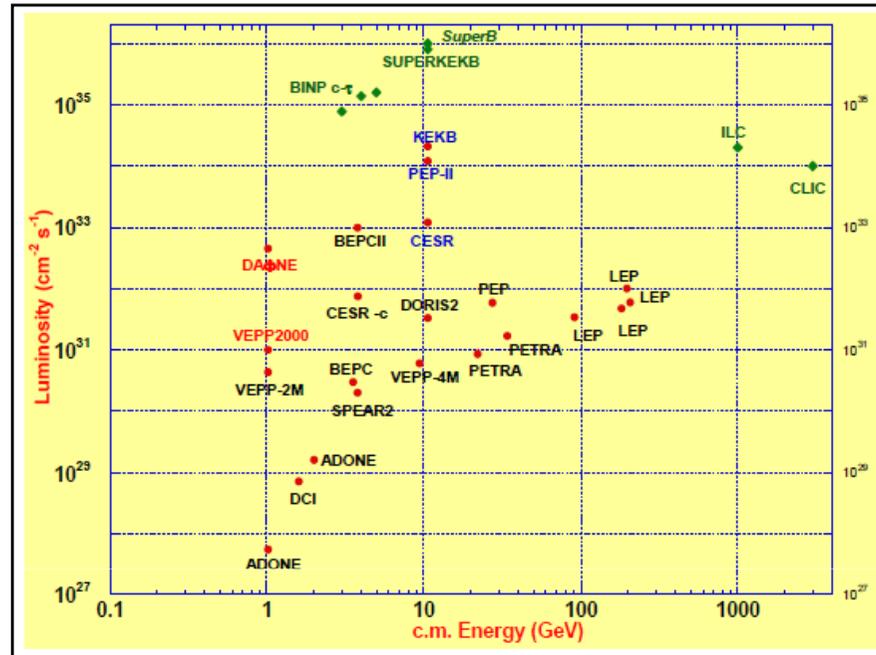
<http://arxiv.org/abs/1009.6178v3>

159 pages

Description of the accelerator systems only

Physical and detector aspects will be in coming documents

# Motivation

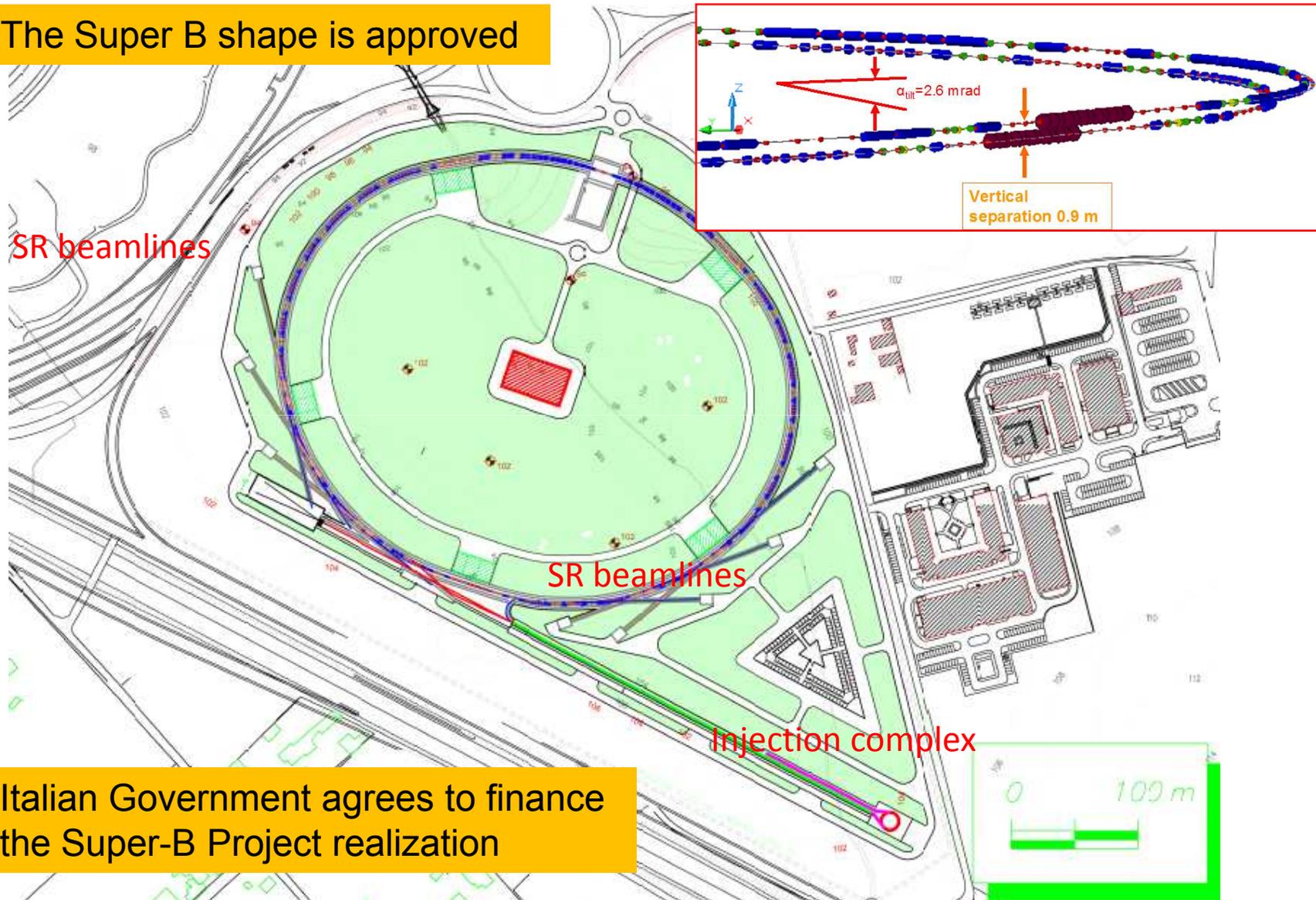


With an integrated luminosity goal larger than 75 ab<sup>-1</sup>, the SuperB factory, to be built on the Tor Vergata Campus, near Roma (Italy) by 2016, has the very ambitious goal to unravel the detailed structure of the new physics soon to be discovered at the LHC, or to explore BSM physics beyond the LHC ... . This goal will be reached using a large number of rare B , charm and tau decays very sensitive to the presence of new heavy particles via virtual loops. ... The challenges in the machine design brought by the requirement of a polarized electron beam will be emphasized.

*(from the abstract at SPIN2012 by Gyu Wormser, LAL , 91989 Orsay France )*

# Schematic SuperB layout

The Super B shape is approved



SR beamlines

SR beamlines

Injection complex

Italian Government agrees to finance the Super-B Project realization

# SuperB parameters

Table 3.1: SuperB parameters for baseline, low emittance and high current options, and for tau/charm running.

Parameter	Units	Base Line		Low Emittance		High Current		Tau-charm	
		HER (e <sup>+</sup> )	LER (e <sup>-</sup> )	HER (e <sup>+</sup> )	LER (e <sup>-</sup> )	HER (e <sup>+</sup> )	LER (e <sup>-</sup> )	HER (e <sup>+</sup> )	LER (e <sup>-</sup> )
LUMINOSITY	cm <sup>-2</sup> s <sup>-1</sup>	1.00E+36		1.00E+36		1.00E+36		1.00E+35	
Energy	GeV	6.7	4.18	6.7	4.18	6.7	4.18	2.58	1.61
Circumference	m	1258.4		1258.4		1258.4		1258.4	
X-Angle (full)	mrad	66		66		66		66	
$\beta_x$ @ IP	cm	2.6	3.2	2.6	3.2	5.06	6.22	6.76	8.32
$\beta_y$ @ IP	cm	0.0253	0.0205	0.0179	0.0145	0.0292	0.0237	0.0658	0.0533
Coupling (full current)	%	0.25	0.25	0.25	0.25	0.5	0.5	0.25	0.25
Emittance x (with IBS)	nm	2.00	2.46	1.00	1.23	2.00	2.46	5.20	6.4
Emittance y	pm	5	6.15	2.5	3.075	10	12.3	13	16
Bunch length (full current)	mm	5	5	5	5	4.4	4.4	5	5
Beam current	mA	1892	2447	1460	1888	3094	4000	1365	1766
Buckets distance	#	2		2		1		1	
Ion gap	%	2		2		2		2	
RF frequency	MHz	476		476		476		476	
Revolution frequency	MHz	0.238		0.238		0.238		0.238	
Harmonic number	#	1998		1998		1998		1998	
Number of bunches	#	978		978		1956		1956	
N. Particle/bunch (10 <sup>10</sup> )	#	5.08	6.56	3.92	5.06	4.15	5.36	1.83	2.37
$\sigma_x$ effective	$\mu$ m	165.22	165.30	165.22	165.30	145.60	145.78	166.12	166.67
$\sigma_y$ @ IP	$\mu$ m	0.036	0.036	0.021	0.021	0.054	0.0254	0.092	0.092
Priniski angle	rad	22.88	18.60	32.36	26.30	14.43	11.74	8.80	7.15
$\Sigma_x$ effective	$\mu$ m	233.35		233.35		205.34		233.35	
$\Sigma_y$	$\mu$ m	0.050		0.030		0.076		0.131	
Hourglass reduction factor		0.950		0.950		0.950		0.950	
Tune shift x		0.0021	0.0033	0.0017	0.0025	0.0044	0.0067	0.0052	0.0080
Tune shift y		0.097	0.097	0.0891	0.0892	0.0684	0.0687	0.0909	0.0910
Longitudinal damping time	ns	13.4	20.3	13.4	20.3	13.4	20.3	26.8	40.6
Energy Loss/turn	MeV	2.11	0.865	2.11	0.865	2.11	0.865	0.4	0.17
Momentum compaction (10 <sup>-4</sup> )		4.36	4.05	4.36	4.05	4.36	4.05	4.36	4.05
Energy spread (10 <sup>-4</sup> ) (full current)	dE/E	6.43	7.34	6.43	7.34	6.43	7.34	6.43	7.34
CM energy spread (10 <sup>-4</sup> )	dE/E	5.0		5.0		5.0		5.0	
Total lifetime	min	4.23	4.48	3.05	3	7.08	7.73	11.4	6.8
Total RF Wall Plug Power	MW	16.38		12.37		28.83		2.81	

Novosibirsk group contributes:

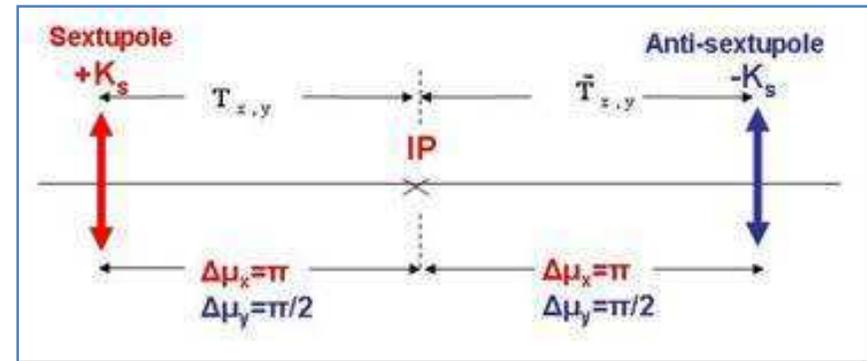
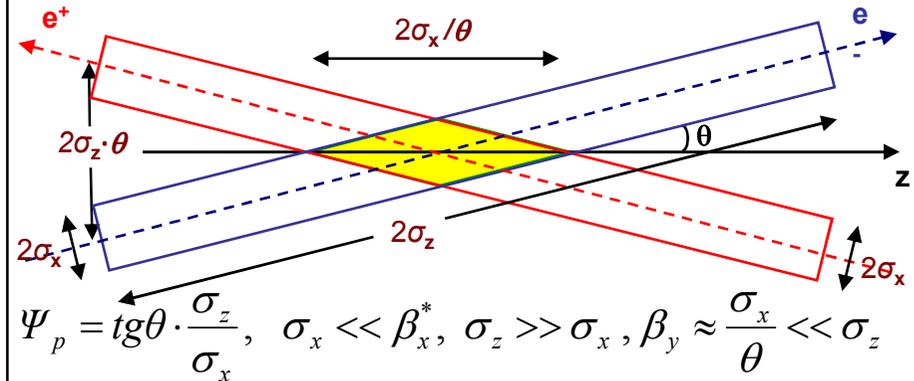
- main ring magnetic structure design
- DA calculation and optimization
- chromaticity correction at FF region
- Beam-Beam simulation
- polarization issues

# Essence of the Crab Waist Collision Scheme

1. **Large Pivinski's angle  $\psi_p$**  greatly shortens the interaction region.
2. Shortening the interaction region allows to decrease considerably the **beta-function** value  $\beta_y^*$  at IP (for instance, 20 times!).
3. On the other hand, the assets 1 and 2 lead to a strong vertical betatron phase modulation at IP by the horizontal betatron oscillations (the coupling resonances  $mQ_x+nQ_y=k$  due to Beam-Beam). To suppress that negative impact the system of two **crab sextupole** is applied. Their forces and locations are chosen in such a way that the vertical phase advance from the sextupole azimuth to the "**collision point**" does not depend upon the horizontal coordinate of particles at that azimuth.

1. P. Raimondi, "Status of the SuperB Effort", presented at the 2nd Workshop on Super B-Factory, LNF-INFN, Frascati, Mar. 2006.

2. P. Raimondi, D. Shatilov, M. Zobov, "Beam-Beam Issues for Colliding Schemes with Large Pivinski Angle and Crabbed Waist", LNF-07/003 (IR), 2007, e-print: arXiv:physics/0702033.



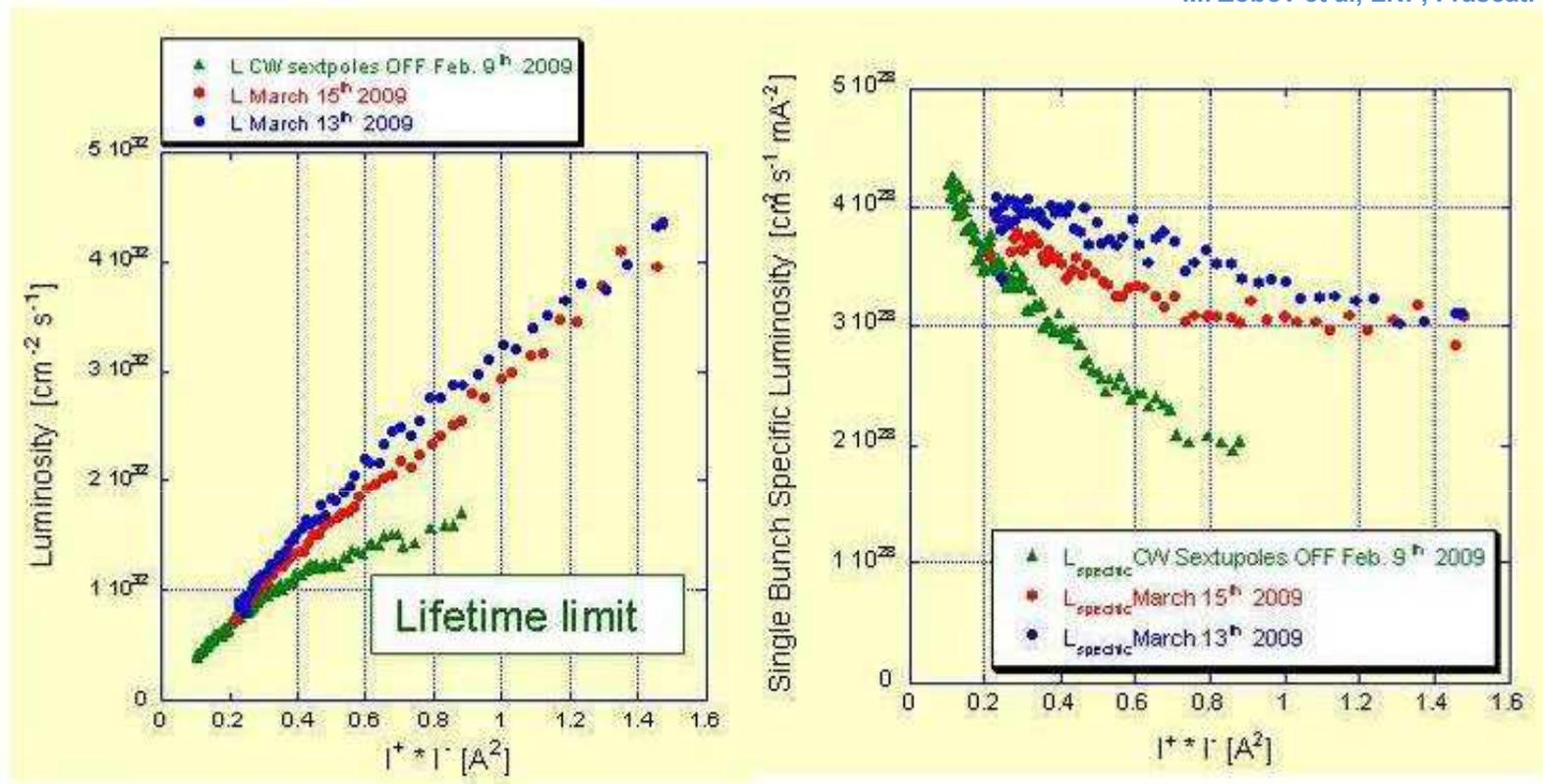
**Increase the maximal beam-beam tune shift and minimize the beta to increase the luminosity:**

$$L \propto \frac{I}{\beta_y^*} \cdot \xi_y$$

Super B:  $\beta_y^*=0.02$  cm + the nominal beam-beam tune shift  $\xi_y=0.1$  at max  $\xi_y=0.2$  (increased due to crab sextupoles)  $\rightarrow$  the beam-beam effects are practically absent!

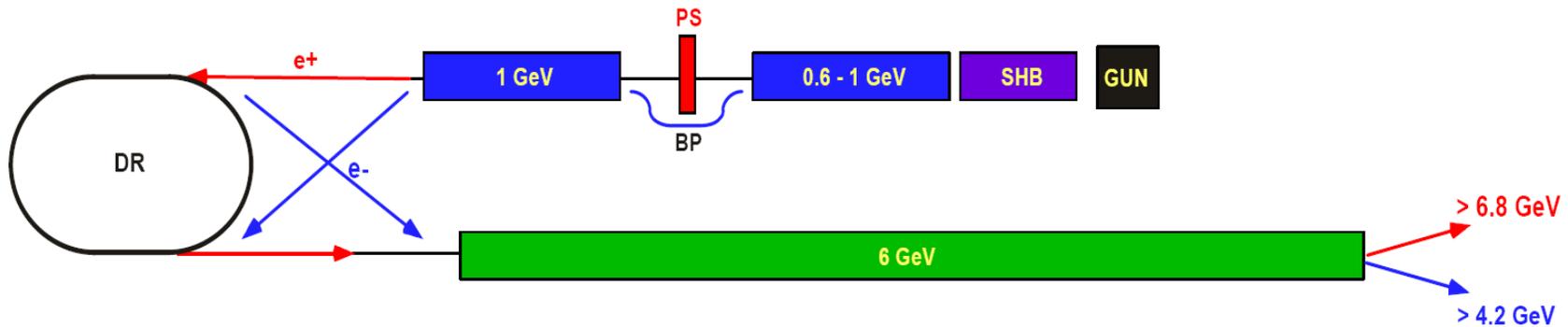
# Test of Crab Waist concept: DAFNE upgrade results

M. Zobov et al, LNF, Frascati

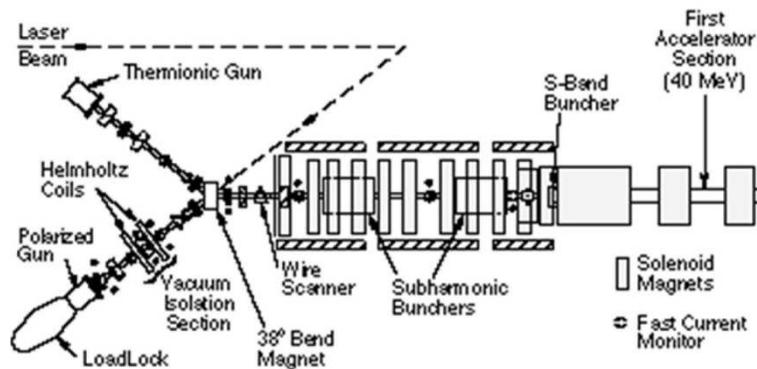


Luminosity vs. product of beam currents (left) and specific luminosity vs. product of beam currents (right), for two record shifts with crab sextupoles ON (red and blue dots) and with crab sextupoles OFF (green)

# Injection Complex



At full luminosity and beam currents, up to 4 A, the Beam Lifetime  $\sim 3-8$  min  $\rightarrow$  continuous injection process (“top-up” injection). Linac operates at 50 Hz. Short train of 5 bunches at a time are produced for each beam type, stored for 20 msec in the shared damping ring and then extracted and accelerated to full injection energy

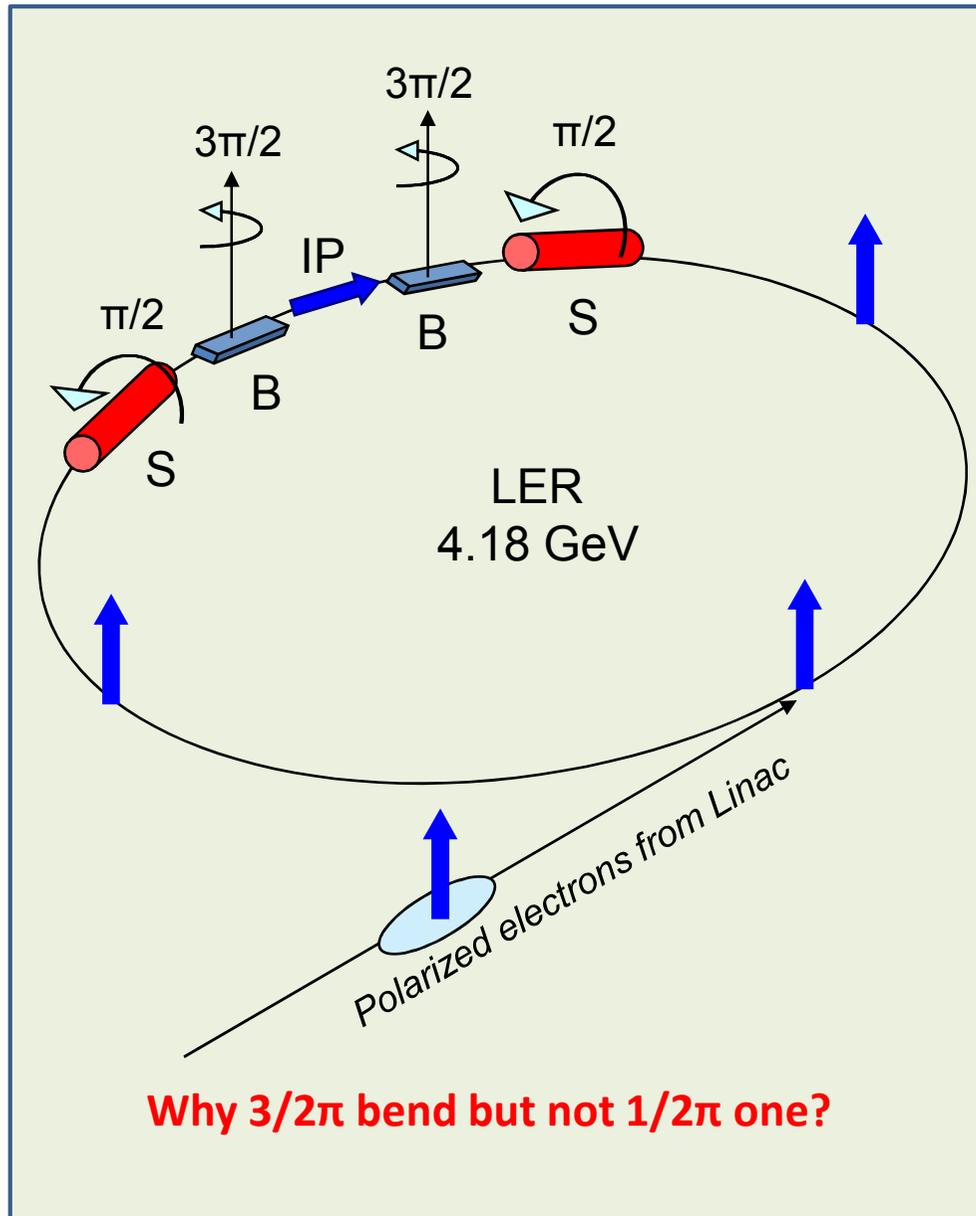


Polarized electron source developed and applied at SLAC

Electrons from the gun source are longitudinally polarized. The spins are rotated to the vertical plane in a special transport section downstream of the gun. At present this section is still under development. Variants under consideration:

- Wien's Filter
- Z-manipulator includes two bends by E-field and solenoids between them

# Spin kinematics and rotators at SuperB

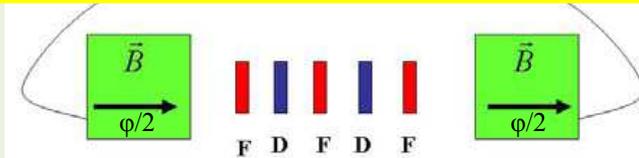


## Solenoid insert optics

Decoupling:  $T = T_x = -T_y$  (V.Litvinenko)

Spin transparency (I.Koop):  
( $r = pc/eB$ )

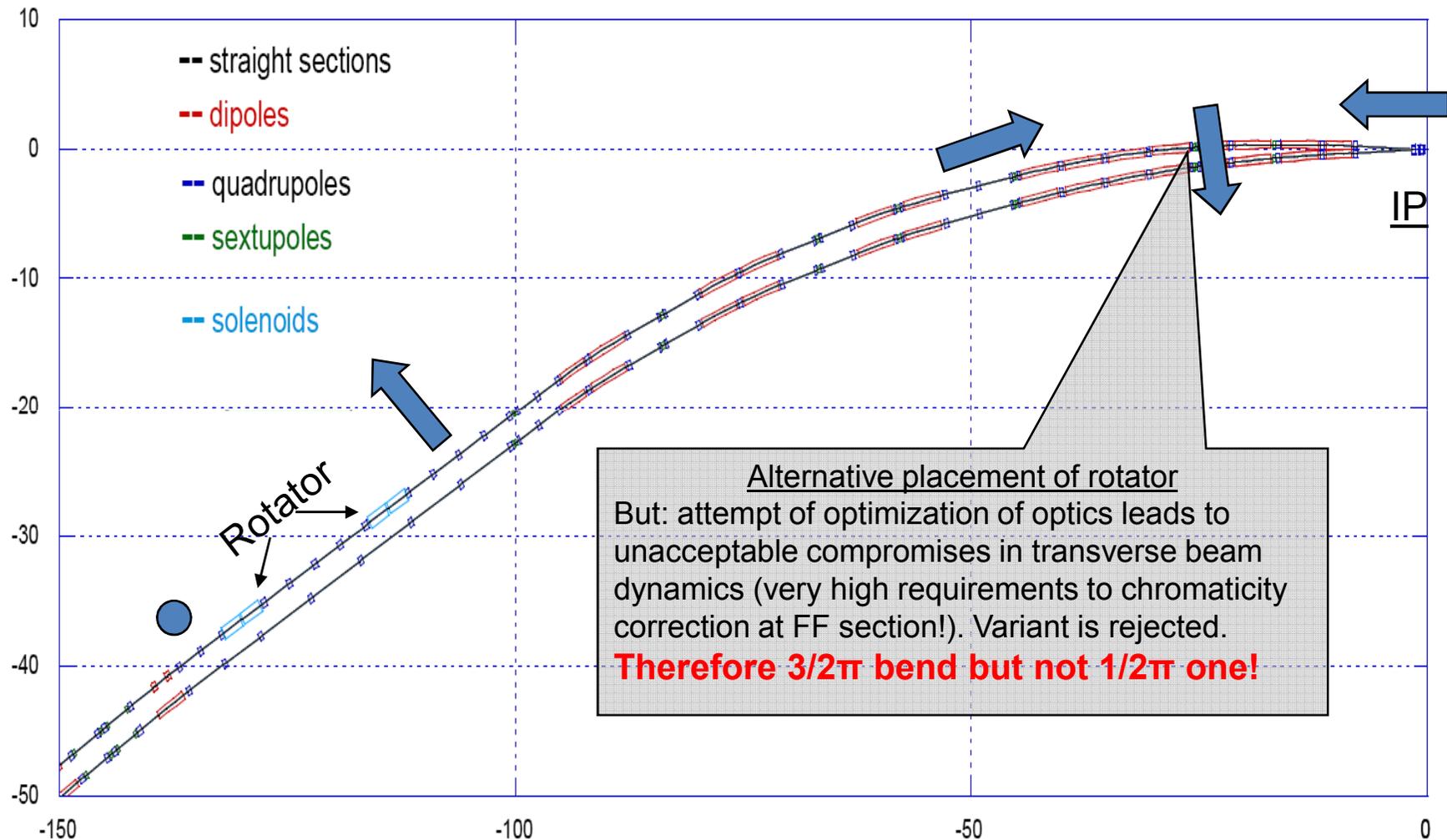
$$T = \begin{vmatrix} -\cos \varphi & -2r \sin \varphi \\ (2r)^{-1} \sin \varphi & -\cos \varphi \end{vmatrix}$$



## Rotator parameters

Parameter	Value	Unit	Comment
Energy	4.18	GeV	
Spin rotation in solenoids	90	°	one side
Solenoid field integral	4 · 10.94	Tm	4 individual solenoids
Solenoid field	2.39	T	
Total length of solenoid section	23.07	m	Includes decoupling optics
Spin rotation of dipoles	270	°	one side
Bending of dipoles	28.4	°	one side

# Layout of the LER Spin Rotator section



# Kinetics of polarization at SuperB

Equilibrium polarization degree under conditions of the continuous injection :

$$P = P_i \cdot \frac{\tau_r}{\tau_r + \tau_l} + P_r \cdot \frac{\tau_l}{\tau_r + \tau_l}$$

$P_i \approx 90\%$  – polarization of the injected portion of particles

$$\tau_r = \tau_0 \cdot \frac{\langle |\dot{\vec{v}}|^3 \rangle}{\left\langle |\dot{\vec{v}}|^3 \left[ 1 - \frac{2}{9} (\vec{n} \cdot \vec{v})^2 + \frac{11}{18} \vec{d}^2 \right] \right\rangle}, \text{ the radiative relaxation time (D - K)}$$

$$\tau_0 [\text{hour}] \approx 2.74 \times 10^{-2} \frac{\rho^2 R [\text{m}^3]}{E^5 [\text{GeV}^5]} \approx 4 \text{ h} @ 4.18 \text{ GeV}, \rho = 29 \text{ m}, R \approx 200 \text{ m}, \text{ the S - T time}$$

$\tau_l$ , the beam life time due to Bhabha Bremsstrahlung at high luminosity ( $\approx 3 - 8$  min)

$$P_r = \frac{8}{5\sqrt{3}} \frac{\langle \dot{\vec{v}}^3 (\vec{n} - \vec{d}) \rangle}{\left\langle |\dot{\vec{v}}|^3 \left[ 1 - \frac{2}{9} (\vec{n} \cdot \vec{v})^2 + \frac{11}{18} \vec{d}^2 \right] \right\rangle} \stackrel{\text{for SuperB}}{\approx} 0.92 \frac{\tau_r}{\tau_0}, \text{ the D - K equilibrium extent}$$

$$P \approx \frac{\tau_r}{\tau_r + \tau_l} \cdot \left( P_i + 0.92 \frac{\tau_r}{\tau_0} \right), \text{ if } \tau_r \ll \tau_0 \text{ and } \tau_r \gg \tau_l, \text{ then } P \rightarrow P_i$$

# Analytic estimate of radiative relaxation time

Main depolarizing factor is a spin-orbit coupling due to Spin Rotators:

$$\tau_r \approx \frac{\tau_0}{1 + \frac{11}{18} \langle \vec{d}^2 \rangle},$$

**Betatron term**

$$\langle \vec{d}^2 \rangle \approx \frac{\langle |h|^2 \rangle [(A\beta_{x,1})^2 + B^2] [1 - \cos 2\pi\nu_0 \cos 2\pi\nu_x]}{4\beta_{x,1} \sin^2 \pi(\nu_x + \nu_0) \sin^2 \pi(\nu_x - \nu_0)} + \frac{D^2}{4 \sin^2 \pi\nu_0}.$$

**Dispersion of spin rotation in bend magnets**

**A** and **B** coefficients are calculated using the transport matrix elements for several points at the solenoid inserts;  $\beta_{x,1}$ , the beta value at input of the insert;  $\langle |h|^2 \rangle$ , the Courant-Snyder's invariant averaged over the arcs

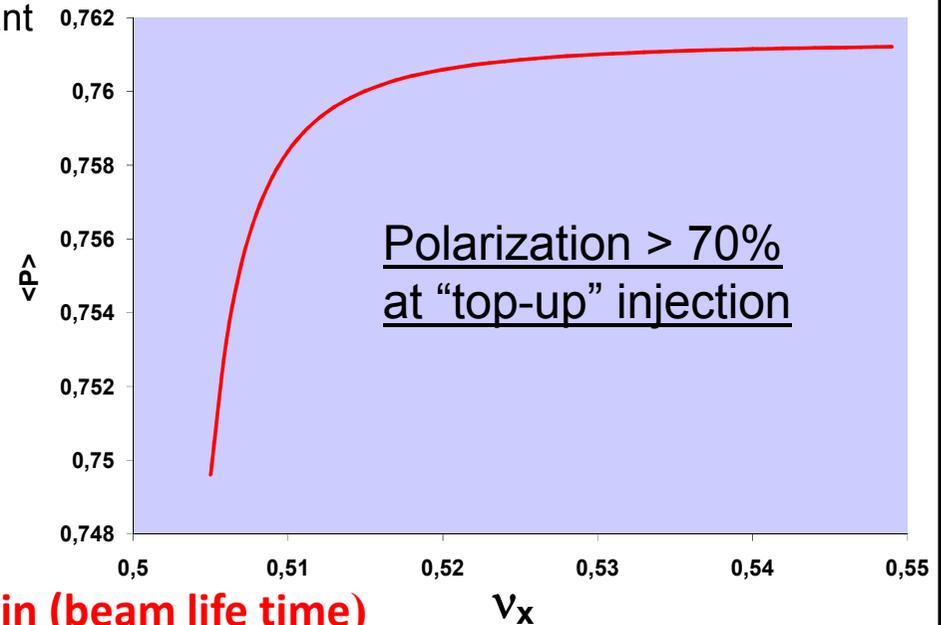
**D=- $\pi$**  spin rotation angle in bend magnets from one rotator to another with IP between and  
**D=-3 $\pi$**  that angle in actual version

Spin tune  $\nu_0 = \nu = \gamma a$  (only for 4.18 GeV)

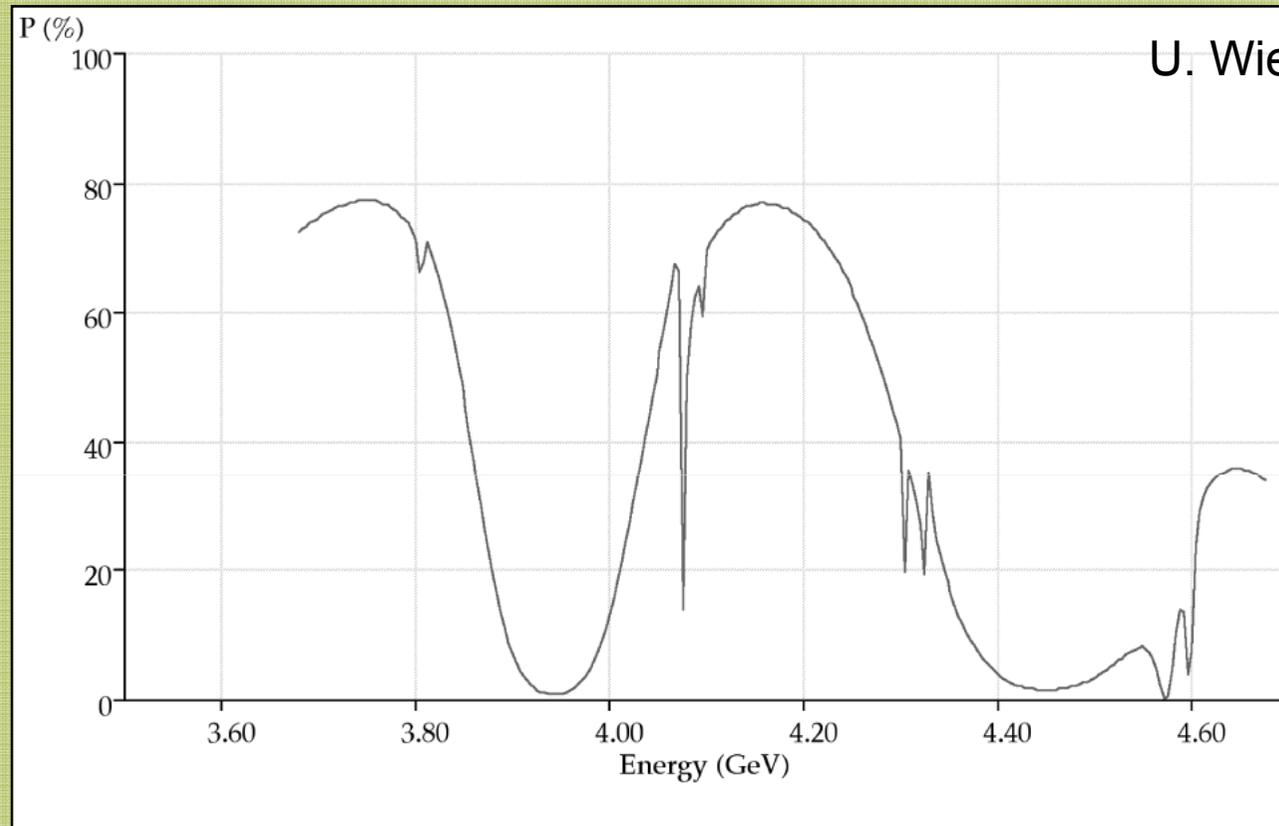
Term with **D** is determinative far from  $\nu_x \pm \nu_0 = k$  resonances where the first term in  $d^2$  matters

**At  $\tau_0 \approx 4h$  and  $D = -3\pi$   $\tau_r = 20 \text{ min} \gg 3 \text{ min}$  (beam life time)**

Time-averaged longitudinal polarization degree at the beam lifetime of 3 min



# Evaluation of equilibrium polarization at SuperB



Code SLICKTRACK (based on approaches of SLIM code by A.Chao)

- comprises a Monte-Carlo spin-orbit tracking algorithm for simulating full 3-d spin-orbit motion in the presence of synchrotron radiation
- limited set of misalignments (in the arcs only) was implemented
- orbit correction was done using a reduced set of correctors.

## Note

Radiative relaxation time  $\tau_r$  is scaled by Sokolov-Ternov time  $\tau_0$  which depends on the arc bend magnet field squared if mean machine radius=const. The larger this field  $\rightarrow$  the smaller  $\tau_0$  and  $\tau_r \rightarrow$  polarization extent drops. At the same time, radiation decrement rises  $\rightarrow$  more easier to achieve low emittance needed for high luminosity. SuperB LER magnetic structure is still under optimization. So, up to date, some current parameters can differ from those in Blue Book.

# Problem of the beam-beam depolarization effect

Very high density of the longitudinally polarized colliding beams makes us to concern about the estimation of beam-beam depolarization (BBD) effect

BBD mechanism is based on the spin resonant diffusion. Spin-orbit resonances of high order may fall into the footprint of the betatron tune shift caused by counter beam field. Tune shift for a given particle is determined by a square of its betatron amplitude – “action”. Incoherent chaotic crossing of the spin resonances due to diffusion and damping processes leads, in principle, to the depolarization effect.

BBD rate was estimated for the first time by [A.M. Kondratenko \(1974\)](#) as applied to conventional storage ring colliders with the vertical polarization. Main conclusion was: [It is possible to conserve the beam polarization provided that BB effects do not crucially disturb the orbital motion \(“no beam blow up”\)](#).

This conclusion needs a quantitative verification *wrt* the features of the Crab Waist IR and the magnetic structure with the polarization rotator inserts.

# About naive approach to BBD

Particle trajectory spread  $\rightarrow$  the polarization decrease in a single pass of IP :

$$\Delta P_{s.p.} \sim \frac{1}{2} \langle \chi^2 \rangle, \chi - \text{an angle of spin rotation in a counter bunch field.}$$

Numerical "single - pass" simulation result discussed at SuperB Meeting, 2010 :

$$\Delta P_{s.p.} \sim 10^{-7} \div 10^{-6}. \text{ Depolarization in } \sim 10^6 \text{ turns (3 sec)?}$$

- Answer is most likely NO. Otherwise one must propose a too short correlation time in orbital and spin motions - from turn to turn (non - realistic!)
- Correlation of spins is limited by rather longer time  $\sim 10$  msec (radiation damping). Over this time, an averaging of all "single - pass" perturbations is available

- Simple estimate :  $\Delta P_{s.p.} \sim \frac{1}{2} \left( \frac{\nu \sigma_y^*}{F_y^*} \right)^2$ ,  $\nu = a\gamma$ ,  $F_y^* \sim \frac{\beta_y^*}{4\pi\xi_y}$  - focal length

Super B (4.2 GeV) :  $\Delta P_{s.p.} \sim 5 \cdot 10^{-7}$  at  $\xi_y \sim 0.1$ ,  $\beta_y^* = 0.02$  cm,  $\nu \approx 10$ ,  $\sigma_y^* \sim 0.02$   $\mu\text{m}$

VEPP - 4M (1.8 GeV) :  $\Delta P_{s.p.} \sim 10^{-7}$  at  $\xi_y \sim 0.04$ ,  $\beta_y^* = 5$  cm,  $\nu \approx 4$ ,  $\sigma_y^* \sim 10$   $\mu\text{m}$

Super and conventional machines do not differ strongly in this parameter!

- Polarization was remaining in luminosity runs at VEPP - 2M, VEPP - 4, SPEAR, HERA
- Obviously, the parameter  $\Delta P_{s.p.}$  can not definitely characterize BBD

# Criterion for the spin-orbit resonances

Caution!  
Here  
Z means  
vertical!

Maximal number  $|k_z|$  of "working" resonance is found from the condition (A.M.Kondratenko, 1974) :  $\nu + k_x \nu_x + k_z \nu_z = k$

$$\lambda_{BBD}^{(k)} \approx \frac{4}{\pi} \cdot \frac{N r_e}{\gamma} \cdot \frac{\nu^2}{\beta_z^*} \cdot |F^\nu|^2 \cdot A \cdot \left[ \frac{\langle a_z^2 \rangle}{\langle a_z^2 \rangle + z_0^2 + z_0 \sqrt{z_0^2 + 2 \langle a_z^2 \rangle}} \right]^{|k_z|} \leq \lambda_r$$

$\langle a_z^2 \rangle$  an averaged square of vertical oscillation amplitude

$z_0$  a vertical beam size

$|F^\nu|_{I.P.}$  Spin Response Function (SRF) shows the spin perturbation amplification/reduction resulting from oscillations excited over the ring by a kick in I.P. (if  $F^\nu \rightarrow 0$  then  $\lambda_{BBD}^{(k)} \rightarrow 0$  for any  $k$ )

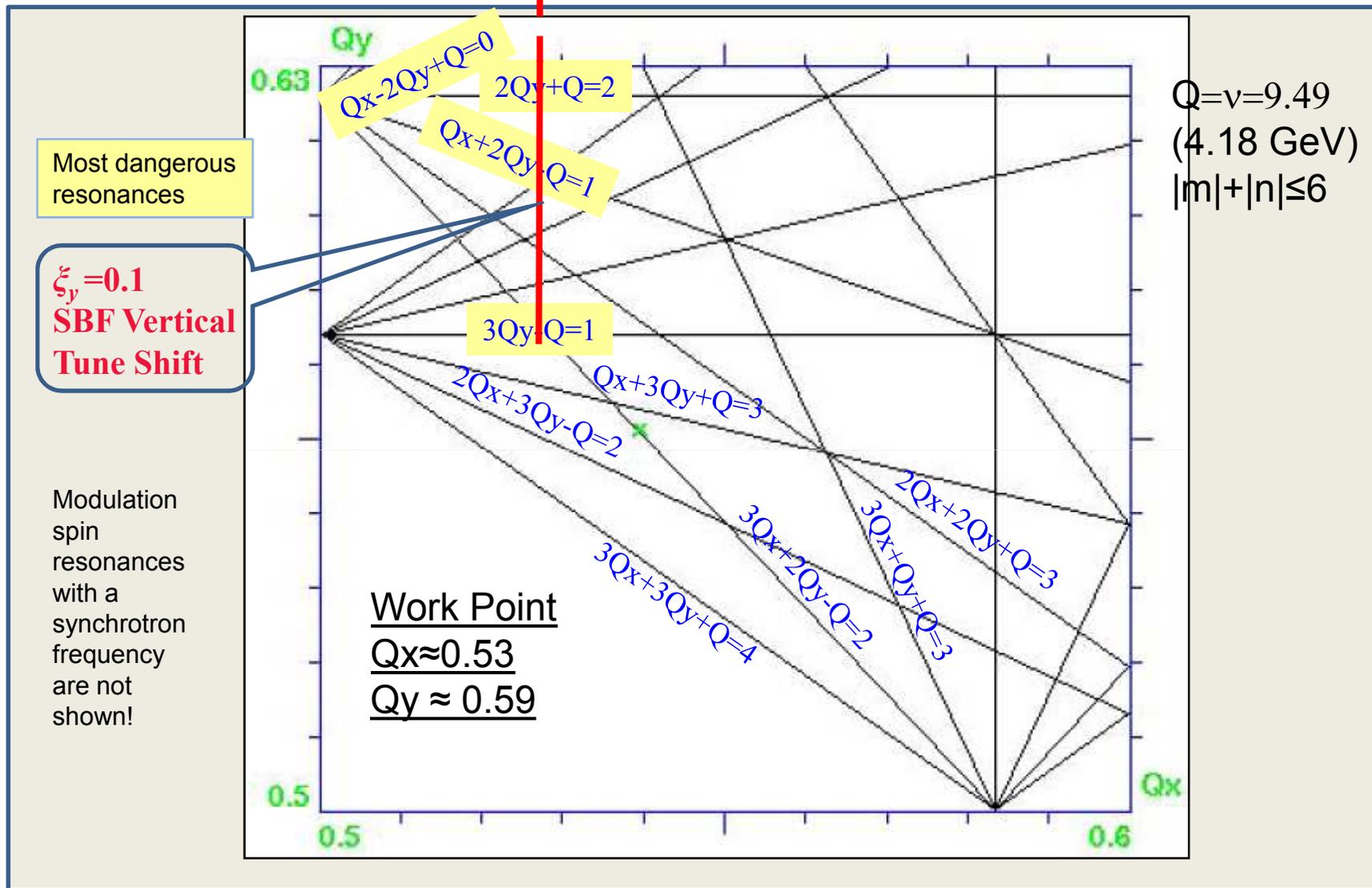
$A$  a factor depending on amplitude distribution

$\lambda_r = \max\{\lambda_{BLT}, 1/\tau_p, \dots\}$  a reference rate  $\sim \lambda_l$

Generally,  $\lambda_{BBD} \sim \sum_k \lambda_{BBD}^{(k)}$ , a sum over all working resonances

**Estimated  $\max\{k_z\}=3$  for case under consideration**

# Spin resonances $Q+mQ_x+nQ_y=k$



**BB footprint may overlap several resonances of the same order!**

# Account of interaction length reduction

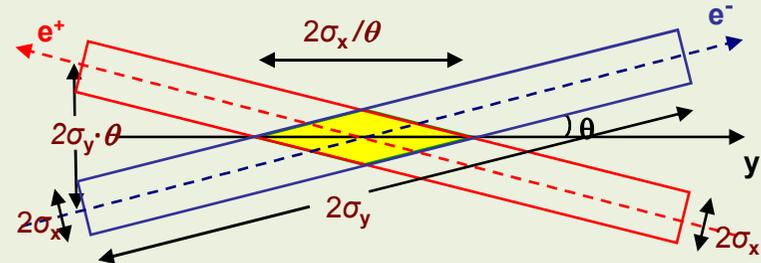
$w_k = 2\nu \langle H_x F^{\nu_k} e^{i\nu_k \tilde{K}_z} \rangle$ , the spin harmonic

$\nu = \nu_k = k + k_z \nu_z + k_x \nu_x$ , the spin resonance condition

$$|w_k| \propto \frac{N_e r_e \nu |F^{\nu_k}|}{\gamma V_b} \cdot l_i,$$

$V_b$ , the counter bunch volume

$$l_i = \begin{cases} \sim \sigma_l, & \text{the beam length (head-on collision)} \\ \sim \frac{\sigma_x}{\theta}, & \text{the interaction length (Crab Waist)} \end{cases}$$



For the resonance  $\nu_k = k + k_z \nu_z$ , the BBD rate is in order  $\lambda_{\text{BBD}} = \frac{1}{\tau_{\text{BBD}}} \sim \frac{\pi \langle |w_k|^2 \rangle}{\sigma_b}$ ,  $\sigma_b = |k_z \cdot \Delta \nu_z|$

$$\Delta \nu_z = \frac{2N_e r_e \beta_z^*}{\pi \gamma \sigma_z^* (\sigma_x^* + \sigma_z^*)} \propto \frac{N_e r_e}{\gamma V_b} \cdot l_i, \quad \text{the tune shift}$$

The higher number  
→ the lower rate

As result,  $\lambda_{\text{BBD}} \propto \frac{N_e r_e \nu^2 |F^{\nu_k}|^2}{\gamma} \times \frac{l_i(\text{CW})}{l_i(\text{head-on})}$ ,  $\frac{l_i(\text{CW})}{l_i(\text{head-on})} \sim \frac{\sigma_x}{\theta \sigma_l} = \frac{1}{\Psi_P}$ ,  $\Psi_P$  – Pivinski's angle

Estimate of  $\lambda_{\text{BBD}}$  by Kondratenko's "head-on" formula reduced by factor  $\frac{1}{\Psi_P} \ll 1$

Caution!  
Here  
Z means  
vertical!

# Summary of BBD features at SuperB Factory

1. The dangerous spin resonances of high order in betatron tunes are unavoidable due to elongated BB foot print. Simultaneously several resonances may be overlapped by the print
2. Very strong collective field of the counter bunch due to very small beam transverse sizes
3. Large Piwinski's angle  $\rightarrow$  length of interaction is reduced (**positive fact!**)
4. Spin perturbations from BB impact in two planes
5. Spin Response Factor (finally increasing or decreasing BBD) determined by excited in IP oscillations depends on the chosen rotator scheme

# Preliminary BBD rate estimates

Collider	E MeV	Beta_x (IP) Cm	Beta_y (IP) Cm	Horizon. Size (IP) Micron	Vertical Size (IP) Micron	Beam Length cm	N per bunch 10 <sup>10</sup>	Cross. Angle (full) mrad	SRF  F <sup>v</sup>   <sup>2</sup>	BBD Time 1/λ <sub>BBD</sub> min
SuperB	4180	2.6	0.0253	7.2	0.036	0.5	5.08	66	1(?)	32
VEPP-4M	1890	70	4	290	4	4.5	2	0	0.08	2500

for  $\nu \pm 3\nu_y = k$ , the considered spin resonance type

Estimate obtained for one of the potentially dangerous resonance is based on unit value of Spin Response Function ( $F^v$ ). That is not realistic, but allows to produce a BBD scaling.

To have a more accurate analysis, we plan in nearest future:

- to calculate an actual value of the SRF for SuperB with longitudinal polarization
- to perform the spin diffusion simulation with account of BB

# BBD simulation

- Usual BB simulation (D.Shatilov) with particle tracking (P.Piminov) over the ring and accounting radiation diffusion and damping
- Turn-to turn evolution of spin vector of model particles in fields of ring and counter bunch
- Find rate  $\langle d S_n/dt \rangle$  of particle ensemble

Spin rotation angle  $\alpha$  of Test Particle  
in the Counter Bunch Slice field:

$$\alpha_z = (1 + \nu) \left( \Delta p_{x'} - \Delta p_{y'} \sin \theta - \frac{\Delta p_{x'}}{1 + \cos \theta} \sin^2 \theta \right),$$

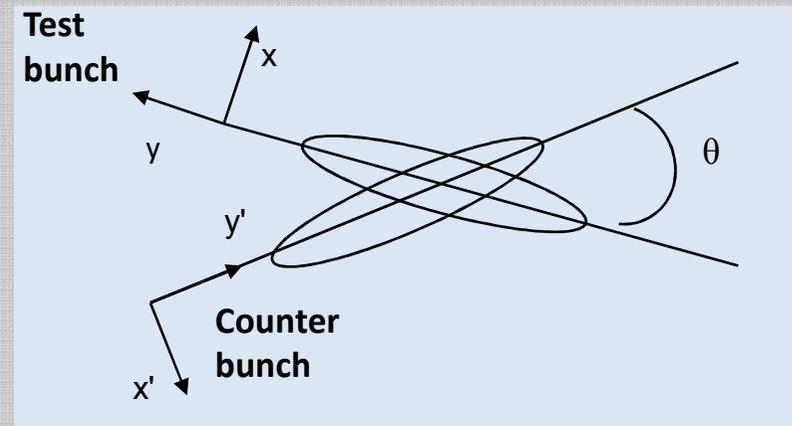
$$\alpha_x = (1 + \nu) \otimes p_z'$$

$$\alpha_y = \frac{\Delta p_{z'}}{1 + \cos \theta} \sin \theta.$$

$\Delta \mathbf{p}$  is increment (r.u.) of test particle momentum  
wrt axes of Counter Bunch reference frame

Spinor transformation at interaction region:

$$M_{bb} = I - \frac{i}{2} (\vec{\sigma} \cdot \vec{\alpha}).$$



# Calculation of Spin Response Function

- **Turn-to-turn simulation using particle tracking and spin rotation matrix algebra (case of a conventional storage ring):**

$$F^v(\theta) = \left\langle -\frac{i \cdot e^{-i2\pi v \cdot N}}{v \cdot h} \cdot \delta S_{\perp}^{(k)} \right\rangle - 1$$

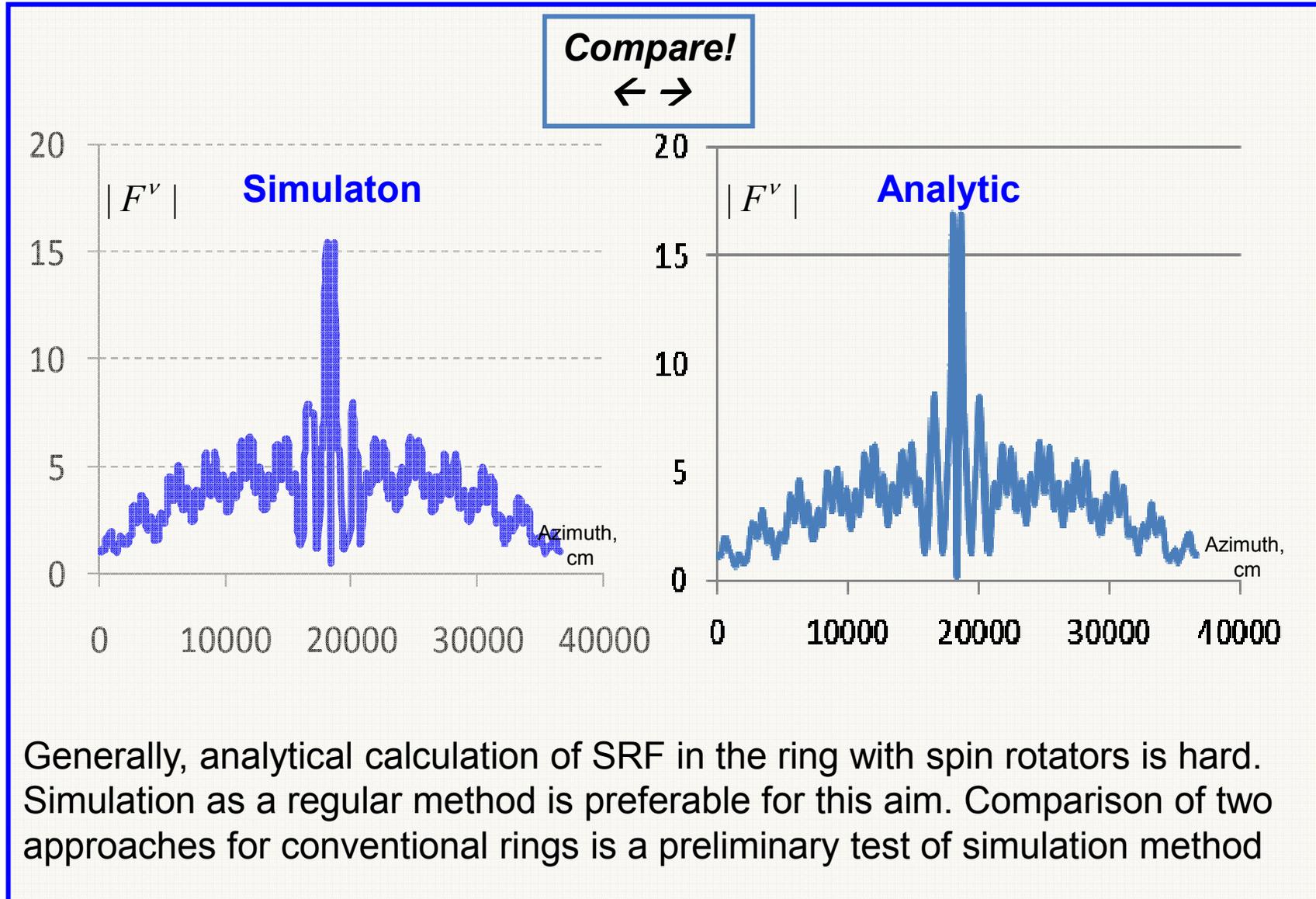
$\delta S_{\perp}^{(k)}$  – a spin vector perturbation transverse to  $\vec{n}$  at  $k$ th turn after a vertical kick of strength  $h$  at an azimuth  $\theta$ ;  $N \gg 1$ , number of turns done;  $\langle \dots \rangle$ , averaging over turns. No damping and diffusion required

- **Analytic approach based on solving the spin precession equations. In particular, there is the Derbenev-Kondratenko formula for SRF valid for conventional storage rings:**

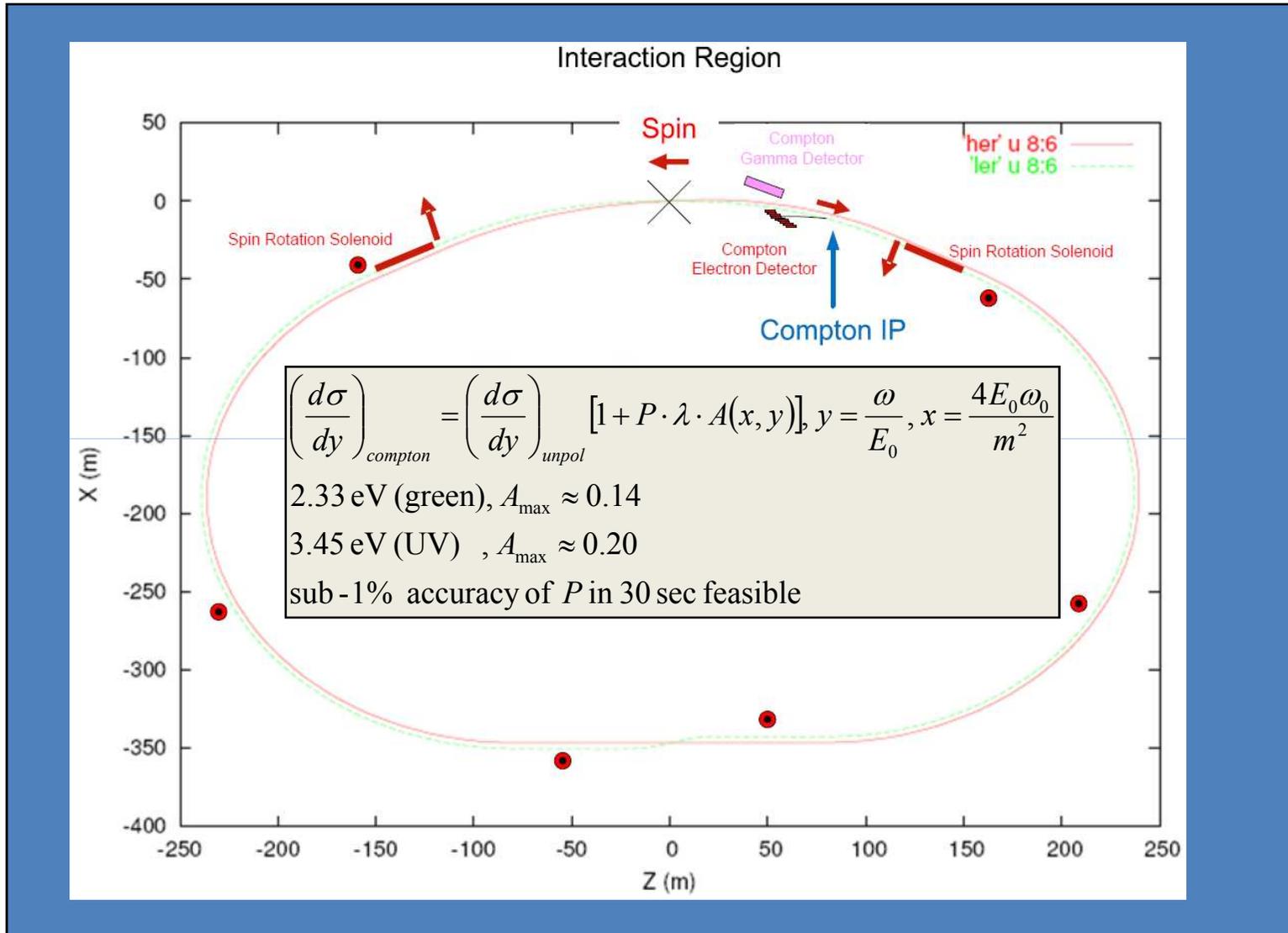
$$F^v \approx \frac{v \cdot e^{i\nu\theta}}{2} \left\{ \left[ 1 - e^{\frac{i2\pi}{m}(\nu+\nu_z)} \right]^{-1} \cdot f_z \int_{\theta-\frac{2\pi}{m}}^{\theta} K f_z^* e^{-i\nu\Phi} d\theta' - \left[ 1 - e^{\frac{i2\pi}{m}(\nu-\nu_z)} \right]^{-1} \cdot f_z^* \int_{\theta-\frac{2\pi}{m}}^{\theta} K f_z' e^{-i\nu\Phi} d\theta' \right\}$$

$f_z(\theta)$ , vertical Floquet function;  $\nu_z$ , vertical betatron tune;  $K(\theta)$ , orbit curvature;  $m$ , number of super - periods

# Test of SRF simulation for 1.84 GeV VEPP-4M



# Compton polarimeter



# Summary

- Preliminary variant of the SuperB Project in all accelerator aspects is elaborated and exists now in the document
- Territory of Tor Vergato Univ. near Rome is approved as a place for SuperB
- Italian Government made a decision to finance SuperB
- International SuperB Team of accelerator physicists is formed and is in activity
- Contribution of Novosibirsk Group from BINP is one of determinative
- Longitudinal polarization scheme is determined and studied. Its optimization is in progress
- Study of Beam-Beam depolarization effect at SuperB started
- Compton polarimeter is implied to measure longitudinal polarization of electrons in LER SuperB

Thank you!